

School of Basic Sciences

Department of Basic Sciences

Mid Term Examination

Exam Date: 05 Oct 2023

Time : 90 Minutes

Marks : 50

Sem V - C1UC502T - Transforms and Calculus of variation

Your answer should be specific to the question asked

Draw neat labeled diagrams wherever necessary

- 1) Define unilateral series. K2 (2)
- 2) Explain the Fast Fourier transform with an example. K1 (3)
- 3) Determine the inverse Z –Transform $e^{-\frac{3}{z}}$. K2 (4)
- 4) Discuss the Z –Transform of $(-3)^n$. K2 (6)
- 5) Using Convolution find $Z^{-1}\left[\frac{z^2}{(z-2)(z-3)}\right]$ K3 (6)
- 6) Find the extremal of the functionals $\int_0^{\frac{\pi}{2}} (y'^2 - y^2 + 2xy) dx$ with $y(\frac{\pi}{2})=0$ and $y(0)=0$ K3 (9)
- 7) Show the Fourier transform of the function $f(t) = e^{-a|t|}$, $-\infty < t < \infty$, $a > 0$ K4 (8)
- 8) Find the extremals $\int_0^{2\pi} \left[\left(\frac{dy}{dx}\right)^2 - y^2 \right] dx$ K4 (12)

OR

Write the extremal of the functional $\int_{x_0}^{x_1} (x^2 - y''^2 + 16y^2) dx$ K4 (12)