

School of Basic Sciences

Master of Science in Physics
Mid Term Examination - Nov 2023

Duration : 90 Minutes
Max Marks : 50

Sem I - C1PO102T - Quantum Mechanics-I

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Interpret Hilbert Space. K2 (2)
- 2) Why wave function should be normalised? K1 (3)
- 3) Interpret acceptable characteristics of wave function. K2 (4)
- 4) Why the following wave function for any value of x are good acceptable wave function? (a) $2\sin x$ (b) $\exp(-x^2)$ K2 (6)
- 5) Consider an ensemble of 100 identical systems, each in state $|\psi\rangle = \frac{2}{\sqrt{5}}|\phi_0\rangle - \frac{1}{\sqrt{5}}|\phi_1\rangle$. Here $|\phi_0\rangle$ and $|\phi_1\rangle$ are the normalized eigenfunctions in ground and excited state respectively. If measurements are done, how many systems will be found in the ground state and excited state? K3 (6)
- 6) Consider a system which is described by the state K3 (9)

$$\psi(\theta, \varphi) = \sqrt{\frac{3}{8}}Y_{11}(\theta, \varphi) + \sqrt{\frac{1}{8}}Y_{10}(\theta, \varphi) + AY_{1,-1}(\theta, \varphi),$$

where A is a real constant

 - (a) Calculate A so that $|\psi\rangle$ is normalized.
 - (b) Find $\hat{L}_+\psi(\theta, \varphi)$.
 - (c) Calculate the expectation values of \hat{L}_x and \hat{L}^2 in the state $|\psi\rangle$.
- 7) Calculate the commutation relation: $[y, L_y]$ K4 (8)

8)

K4 (12)

At time $t=0$, a particle is represented by:

$$\psi(x,0) = \begin{cases} Ax/a & \text{if } 0 \leq x \leq a \\ A \left(\frac{b-x}{b-a} \right) & \text{if } a \leq x \leq b \\ 0 & \text{otherwise} \end{cases}$$

Here A, a and b are constants.

- What is normalized value of ψ ?
- Sketch $\psi(x,0)$ as a function of x.
- Where is the particle most likely to be found at $t=0$?
- Probability of finding the particle left of a. what is probability if $b=a$ and $b=2a$?

OR

Consider a wave function:

K4 (12)

$$\psi(x,t) = Ae^{-\lambda|x|} e^{-i\omega t}$$

Find the value of A (b) Determine expectation value of x and x^2 . (c) Plot $|\psi|^2$