

ADMISSION NUMBER											

**School of Basic Sciences**  
Bachelor of Science Honours in Mathematics  
Mid Term Examination - Nov 2023

Duration : 90 Minutes  
Max Marks : 50

**Sem I - C1UC101T - Algebra**

General Instructions

*Answer to the specific question asked*

*Draw neat, labelled diagrams wherever necessary*

*Approved data hand books are allowed subject to verification by the Invigilator*

- 1) Explain One-to-one correspondence of a function. K2 (2)
- 2) Find whether the given relation on set A is reflexive, symmetric, transitive or not. K1 (3)  
 Let  $A = \{1, 2, 3, 4\}$   
 $R_1 = \{(1, 1), (2, 2), (3, 3), (4, 4), (1, 2), (2, 1), (2, 3), (3, 2)\}$ ,  
 $R_2 = \{(1, 1), (2, 2), (3, 3), (4, 4), (1, 2), (2, 1), (2, 3), (3, 2)\}$ .
- 3) Estimate the number that should be added to  $x^2 + 5$  so that the resulting polynomial leaves the remainder 3 when divided by  $x + 3$  ? K2 (4)
- 4) Show that the relation of equality on integers is an equivalence relation K2 (6)
- 5) Use the Division Algorithm to establish the following: The fourth power of any integer is either of the form  $5k$  or  $5k + 1$ . K3 (6)
- 6) Prove that a map  $f$  is invertible iff it is one-one onto. K3 (9)
- 7) Use the Division Algorithm to establish the following: The square of any integer is either of the form  $3k$  or  $3k + 1$  K4 (8)
- 8) Examine the validity of the statement: For any integer  $a$ ,  $a^3 \equiv 0, 1, \text{ or } 8 \pmod{9}$  K4 (12)

**OR**

Examine the validity of the following statement: If  $a \mid (b + c)$ , then either  $a \mid b$  or  $a \mid c$  K4 (12)