

--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

School of Basic Sciences
Bachelor of Science Honours in Mathematics
Mid Term Examination - Mar 2024

Duration : 90 Minutes
Max Marks : 50

Sem VI - C1UC601T - Metric Spaces and Complex Analysis

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Explain that every convergent sequence is cauchy sequence. K2 (2)
- 2) Find the limit point of a set $A = \{1, 1/2, 1/3, 1/4, 1/5, 1/6, \dots 1/n, \dots\}$, $n \in \mathbb{N}$ in a usual metric space (\mathbb{R}, d) and justify your answer. K1 (3)
- 3) Estimate the relationship between compactness and sequential compactness in a metric space. K2 (4)
- 4) Show that arbitrary union of any collection of open sets in a metric space is open while arbitrary intersection need not. K2 (6)
- 5) Show that the identity map from any metric space to itself is continuous. K3 (6)
- 6) Verify that a compact metric space is bounded while a bounded metric space need not compact K3 (9)
- 7) Categorize the following metric spaces into compact and non compact metric spaces and justify your answers: (i) (\mathbb{R}, d) (ii) $[0, 1], d$ where d is usual metric. K4 (8)
- 8) Examine whether union and intersection of two compact subsets of a metric space is compact or not. K4 (12)

OR

Examine whether arbitrary union and intersection of closed sets in a metric space is closed or not. K4 (12)