

School of Basic Sciences

Master of Science in Physics
Mid Term Examination - May 2024

Duration : 90 Minutes
Max Marks : 50

Sem II - C1PO202T - Quantum Mechanics-II

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Interpret the properties of spherical harmonics. K2 (2)
- 2) Explain the Perturbation theory. K1 (3)
- 3) Explain the properties of spherical harmonics. K2 (4)
- 4) Calculate the first order correction to the ground state energy of an harmonic oscillator of K2 (6)

mass m and angular frequency ω subjected to a potential $V(x) = 1/2 m\omega^2 x^2 + bx^n$, where b is a parameter independent of x . The ground state wave function is

$$\psi_0^0 = \left(\frac{m\omega}{\pi\hbar} \right)^{1/4} \exp \left(-\frac{m\omega x^2}{2\hbar} \right)$$

- 5) Build the splitting energy level diagram due to L-S coupling in weak magnetic field. K3 (6)
- 6) Obtain the first order correction in energy and wavefunction for $V = bx^3$ K3 (9)
- 7) K4 (8)

Calculate the differential cross section in the first Born approximation for the scattering between two identical particles having spin 1, mass m , and interacting through a potential $V(r) = V_0 e^{-ar}$.

Using first-order perturbation theory, calculate the energy of the n th excited state for a spinless particle of mass m moving in an infinite potential well of length $2L$, with walls at $x = 0$ and $x = 2L$:

$$V(x) = \begin{cases} 0, & 0 \leq x \leq 2L, \\ \infty, & \text{otherwise,} \end{cases}$$

which is modified at the bottom by the following two perturbations:

(a) $V_p(x) = \lambda V_0 \sin(\pi x/2L)$; (b) $V_p(x) = \lambda V_0 \delta(x - L)$, where $\lambda \ll 1$.

OR

Consider a system whose Hamiltonian is given by $\hat{H} = E_0 \begin{pmatrix} 1+\lambda & 0 & 0 & 0 \\ 0 & 8 & 0 & 0 \\ 0 & 0 & 3 & -2\lambda \\ 0 & 0 & -2\lambda & 7 \end{pmatrix}$,

where $\lambda \ll 1$.

(a) By decomposing this Hamiltonian into $\hat{H} = \hat{H}_0 + \hat{H}_p$, find the eigenvalues and eigenstates of the unperturbed Hamiltonian \hat{H}_0 .

(b) Diagonalize \hat{H} to find the exact eigenvalues of \hat{H} ; expand each eigenvalue to the second power of λ .