

School of Computing Science and Engineering
Bachelor of Technology in Computer Science and Engineering
Mid Term Examination - May 2024

Duration : 90 Minutes
Max Marks : 50

Sem II - C1UC222B - Engineering Mathematics-II

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Position vector of a moving particle is given by $\mathbf{r}(t) = x(t)\mathbf{i} + y(t)\mathbf{j} + z(t)\mathbf{k}$, where $x(t) = t^2, y(t) = 2t, z(t) = 4$. Find the velocity and acceleration of the particle at (1,2,4). K2 (2)
- 2) Let $T: \mathbb{R}^2 \rightarrow \mathbb{R}$ be a mapping defined by $T(x, y) = x + y$. Show that T defines a linear transformation on \mathbb{R}^2 . K1 (3)
- 3) Define orthogonal set in \mathbb{R}^3 .
Show that the set $\{v_1, v_2, v_3\}$ is an orthogonal set in \mathbb{R}^3 if $v_1 = (2, 1, -1), v_2 = (0, 1, 1), v_3 = (1, -1, 1)$. K2 (4)
- 4) Find a unit normal vector to the surface $xy^2 + 2yz = 8$ at the point (3, -2, 1). K2 (6)
- 5) Let $T: \mathbb{R}^3 \rightarrow \mathbb{R}^3$ be defined as $T(a, b, c) = (0, a, b)$. Prove that $T \neq \hat{0}, T^2 \neq \hat{0}$ but $T^3 = \hat{0}$ K3 (6)
- 6) Show that the vector field $F = 2x(y^2 + z^3)\mathbf{i} + 2x^2y\mathbf{j} + 3z^2x^2\mathbf{k}$ is conservative. Find its potential function. K3 (9)
- 7) Classify the following mappings whether they are linear or non-linear: K4 (8)
 1. $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$ defined by $T(x, y) = (1 + x, y)$;
 2. $T: \mathbb{R}^2 \rightarrow \mathbb{R}$ defined by $T(x, y) = |x - y|$.
- 8) Consider the vectors $u_1 = (1, 1, 1), u_2 = (1, 2, 3)$ and $u_3 = (2, -1, 1)$ in \mathbb{R}^3 . Express $w = (1, -2, 5)$ as a linear combination of u_1, u_2 and u_3 . K4 (12)

OR

Evaluate $\oint_C 3x^2y dx - 2xy^2 dy$, where C is the boundary of the region $x^2 + y^2 \leq 16, x \geq 0, y \geq 0$ by Green's theorem. [Hint: Parametric representation of C is $x = 4 \cos t, y = 4 \sin t; 0 \leq t \leq 2\pi$.] K4 (12)