

School of Computing Science and Engineering

Bachelor of Technology in Computer Science and Engineering

Mid Term Examination - May 2024

Duration : 90 Minutes

Max Marks : 50

Sem VI - E2UC512T - Advanced Numerical Methods

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Discuss cubic spline interpolation K2 (2)
- 2) Find the largest Eigen value and corresponding Eigen vector of the matrix $\begin{bmatrix} 5 & 4 \\ 2 & 2 \end{bmatrix}$ by power methods. K1 (3)
- 3) Define Jacobi method for symmetric matrices. K2 (4)
- 4) Transform the matrix $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$ to tri-diagonal form using Householder's method. K2 (6)
- 5) Solve the equations $x^2 + y = 11$, $y^2 + x = 7$ correct to three decimal places, by applying Newton-Raphson method, given that $x_0 = 3.5$ and $y_0 = -1.8$ K3 (6)
- 6) Obtain the cubic spline for the following data: K3 (9)

x	0	1	2
f(x)	2	-6	-8
- 7) Transform the following matrix into tridiagonal form by using Given's method, reduce $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$ K4 (8)
- 8) Apply Muller's method to find the root of the equation $x^3 + 2x^2 + 10x - 20 = 0$ taking $x_0 = 0, x_1 = 1, x_2 = 2$. K4 (12)

OR

Obtain by power method, the numerically dominant eigen value and eigen vector of the matrix. $\begin{bmatrix} 2 & 3 & 1 \\ 3 & 2 & 2 \\ 1 & 2 & 1 \end{bmatrix}$. K4 (12)