

School of Computing Science and Engineering

Bachelor of Computer Applications
Semester End Examination - Jun 2024

Duration : 180 Minutes
Max Marks : 100

Sem II - E1UA202T / BCAS1204 Probability and Statistics

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Define range. Find the range & coefficient of range: K1 (3)

| Marks | Students |
|-------|----------|
| 0-10 | 12 |
| 10-20 | 18 |
| 20-30 | 27 |
| 30-40 | 20 |
| 40-50 | 17 |
| 50-60 | 6 |

- 2) Define discrete random variables and continuous random variables with examples. K2 (4)

- 3) Consider a random variable X with probability density function K2 (6)

$$f(x) = \begin{cases} 4x^3, & \text{if } 0 < x < 1 \\ 0, & \text{otherwise} \end{cases}$$
 Find E(X) and V(X).

- 4) If X is a binomial random variable with n = 6 and p = 0.13, find the following values, expressed to 4 decimal places. K3 (6)

- a) P (X = 4)
- b) P (X ≥ 4)
- c) P (X < 4)

- 5) Calculate the probability for the random variable 5 using normal distribution with the population mean is 2 and standard deviation is 3. K3 (6)

- 6) The probability of X, Y, Z became managers are 4/9, 2/9, & 1/3 respectively. The probabilities that the bonus scheme will be introduced if X, Y, and Z becomes managers are 3/10, 1/2, & 4/5 respectively. K3 (9)

- (a) What is the probability that bonus schemes will be introduced.
- (b) If the bonus scheme has been introduced, what is the probability that the manager appointed was X?

- 7) X is a normally distributed variable with mean $\mu = 30$ and standard deviation $\sigma = 4$. Find the probabilities K3 (9)
- $P(X < 40)$
 - $P(X > 21)$
 - $P(30 < X < 35)$

- 8) A manufacturer produces light – bulbs that are packed into boxes of 100. If quality control studies indicate that 0.5% of the light-bulbs produced are defective, examine the percentage of the boxes will contain: K4 (8)
- no defective?
 - 2 or more defectives?

- 9) Find the means of X and Y variables and the coefficient of correlation between them from the following two regression equations: K4 (12)
- $$4X - 5Y + 33 = 0,$$
- $$20X - 9Y - 107 = 0$$

- 10) (a) Find the t-test value for the following two sets of values: 7, 2, 9, 8 and 1, 2, 3, 4? K5 (10)
- (b) A sample of 10 boxes of chips is drawn in which the mean weight is 490 gm and the standard deviation of the weight is 9 gm. Can the sample be considered to have come from population having mean weight 500 gm.

- 11) Find the standard deviation of the following data 7, 4, 8, 10, 11. Add 3 to all the values then find the standard deviation for the new values. K5 (15)

OR

Construct the simple linear regression equation of Y on X if K5 (15)

$$n = 7, \sum_{i=1}^n x_i = 113, \sum_{i=1}^n y_i = 182, \sum_{i=1}^n x_i^2 = 1983, \sum_{i=1}^n x_i y_i = 3186$$

- 12) For the random variable X with the given probability mass function as below, find the mean and variance. K6 (12)

$$f(x) = \begin{cases} 2(x-1) & 1 < x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

OR

The mean lifetime of 200 fluorescent light bulbs produced by a company is computed to be 3140 hours with a standard deviation of 240 hours. Check if there is any difference between population and sample mean using a 5% level of significance. K6 (12)