

## School of Engineering

**M.Tech Structural Engineering  
Semester End Examination - Jun 2024**

**Duration : 180 Minutes  
Max Marks : 100**

### Sem II - G1PC202T - Theory of Elasticity and Plasticity

General Instructions

*Answer to the specific question asked*

*Draw neat, labelled diagrams wherever necessary*

*Approved data hand books are allowed subject to verification by the Invigilator*

- 1) Recall and explain Vonmises theory K1(2)
- 2) Explain Airy's Stress Function. K2(4)
- 3) Illustrate maximum Principal Stress theory K2(6)
- 4) Solve the following problem: The following is the stress tensor is given according to cartesian coordinate system. The Coordinate system is rotated about z axis in anticlockwise direction to about 30 degree. Determine the new stress components.  $\sigma_x=50$  MPa;  $\sigma_y=30$  MPa;  $\sigma_z=15$  MPa;  $\tau_{xy}=20$  MPa;  $\tau_{yz}=5$  MPa ;  $\tau_{xz}=10$ MPa. K3(9)
- 5) Construct the octaheral planes and prove the following. K3(9)  

$$\tau_{oct}^2 = \frac{1}{9}[(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2]$$
- 6) The components of strain tensor in matrix form is given as follows: K5(10)  

$$\begin{bmatrix} 0.001 & 0.002 & 0.005 \\ 0.002 & 0.003 & 0.004 \\ 0.005 & 0.004 & 0.005 \end{bmatrix}$$

Find the octahedral and normal shear strain.
- 7) Examine the following problem: At a point in a material, the state of stress in MPa is given by the components  $\sigma_x = 12.8$ ,  $\sigma_y = 27$ ,  $\sigma_z = 51.3$ ,  $\tau_{xy} = 23.4$ ,  $\tau_{yz} = -6.24$  and  $\tau_{xz} = 11$  Determine the normal and shear stresses on a plane whose normal makes angles of  $48^\circ$  and  $71^\circ$  to the x and y axes respectively. K4(12)
- 8) The state of stress at a point is given by the following matrix. K5(15)  

$$\sigma_{ij} = \begin{bmatrix} 9 & 6 & 3 \\ 6 & 5 & 2 \\ 3 & 2 & 4 \end{bmatrix}$$

Determine the principal stresses and principal directions.
- 9) An I section with flanges 10 cm  $\times$  2 cm and web 28 cm  $\times$  1 cm is subjected to a torque = 2 kNm. Find the maximum shear stress and angle of twist per unit length.  $G = 80,000$  N/Sq.mm K5(15)
- 10) Consider the bar of cast iron under complex loading. The bar is subjected to BM of 39 N-m and twisting moment of  $T = 225$  N-m. Diameter of the bar is 20mm. The bar yields at yield stress 128 MPa in simple tension test. Analyse whether the bar will fail according to maximum principal stress criterion. K6(18)