

Course Code : BSCS2315 Course Name: Design and Analysis of Algorithms

UNIT II DIVIDE-AND-CONQUER

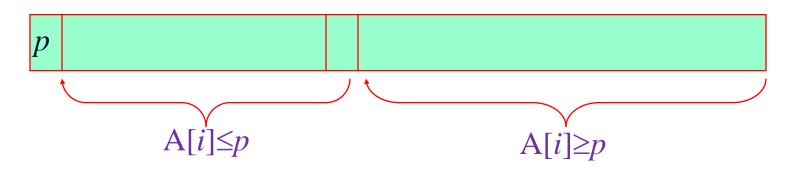
Divide and Conquer Methodology – Binary Search – **Merge Sort** – Quick Sort – Heap Sort – Multiplication of Large Integers – Strassen's Matrix Multiplication



Course Code : BSCS2315 Course Name: Design and Analysis of Algorithms

Quicksort

- **Select** a *pivot* (partitioning element) here, the first element
- Rearrange the list so that all the elements in the first *s* positions are smaller than or equal to the pivot and all the elements in the remaining *n*-*s* positions are larger than or equal to the pivot (see next slide for an algorithm)



□ Exchange the pivot with the last element in the first (i.e., ≤) subarray — the pivot is now in its final position

Sort the two subarrays recursively



School of Computing Science and Engineering

Course Code : BSCS2315 Course Name: Design and Analysis of Algorithms

Partitioning Algorithm

```
Algorithm Partition(A[l.r])
//Partitions a subarray by using its first element as a pivot
//Input: A subarray A[l..r] of A[0..n-1], defined by its left and right
           indices l and r (l < r)
//Output: A partition of A[l..r], with the split position returned as
            this function's value
p \leftarrow A[l]
i \leftarrow l; \quad j \leftarrow r+1
repeat
    repeat i \leftarrow i+1 until A[i] > p
    repeat j \leftarrow j - 1 until A[j] + p
    swap(A[i], A[j])
until i \geq j
\operatorname{swap}(A[i], A[j]) \ / \ / \ undo \ last \ swap \ when \ i \ge j
swap(A[l], A[j])
return j
                                Time complexity: \Theta(l-r) comparisons
```



School of Computing Science and Engineering

Course Code : BSCS2315 Course Name: Design and Analysis of Algorithms

Quicksort Example

- 5 3 1 9 8 2 4 7
- 2 3 1 4 5 8 9 7
- 1 2 3 4 5 7 8 9
- 1 2 3 4 5 7 8 9
- 1 2 3 4 5 7 8 9

1 2 3 4 5 7 8 9



Course Code : BSCS2315 Course Name: Design and Analysis of Algorithms

Analysis of Quicksort

- **Best case: split in the middle** $\Theta(n \log n)$
- **U** Worst case: sorted array! $\Theta(n^2)$
- **Average case: random arrays** $\Theta(n \log n)$
- Improvements:
 - better pivot selection: median of three partitioning
 - switch to insertion sort on small subfiles
 - elimination of recursion

These combine to 20-25% improvement

□ Considered the method of choice for internal sorting of large files (n ≥ 10000)

